Hi (name)  
I'd like to say thank you for my recent promotion. I'm excited to start the role of (position). I will repay your faith in me by performing to the fullest of my abilities.  
I understand you faced a difficult decision in making your appointment, and I am encouraged that I am your choice.  
I won't let you down.  
Best regards,  
(Your name)